

Towards Safe and Reliable CPS: a Learning-based Distributed Fault-Diagnosis Approach

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A few definitions from the literature

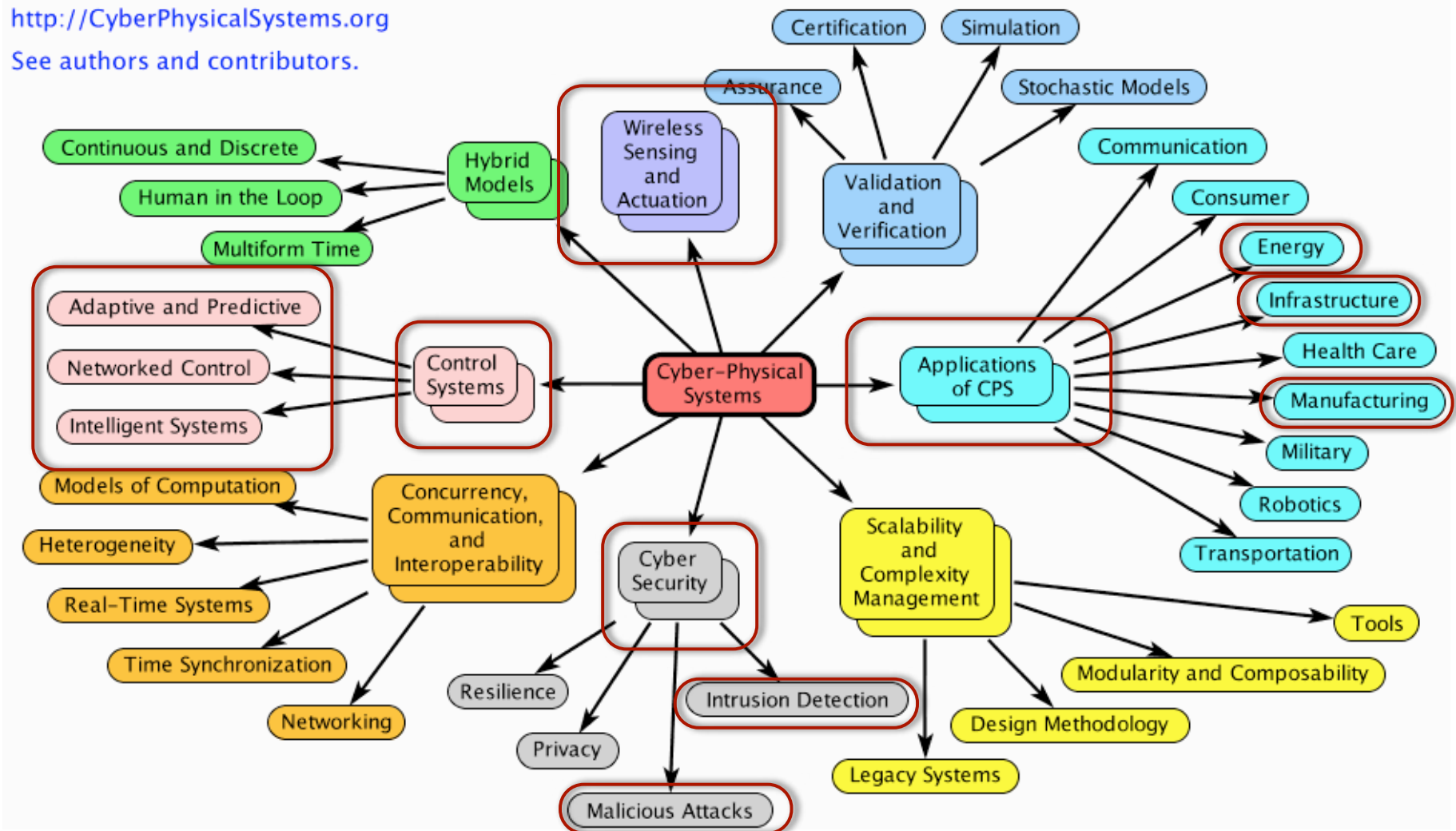
- CPS are engineered systems whose operations are **monitored**, coordinated, controlled, and integrated by a computing and communication core embedded in all types of objects and structures in the physical environment
- CPS usually comprise a network of physically distributed embedded sensors and actuators equipped with **computing** and **communicating** capabilities. Although each individual device is fairly inept at monitoring or regulating the physical substratum, the **coordinated action** of the individual network nodes has the potential for unprecedented capabilities
- CPSs refer to the next generation of engineered systems that require tight integration of computing, communication, and control technologies to achieve stability, performance, **reliability**, **dependability**, **fault-tolerance**, robustness, and efficiency in dealing with physical systems of many application domains

CPSs

Cyber-Physical Systems – a Concept Map

<http://CyberPhysicalSystems.org>

See authors and contributors.



Monitoring and fault diagnosis of CPSs

Motivations

- Huge recent interest in research and applications into reliable methods for **diagnosing faults in complex systems**
- High levels of **safety, performance, reliability, dependability, and availability** are needed in several application domains
- **Faults**: off-specification production, increased operating costs, chance of line shutdown, danger for humans, detrimental environmental impact, ...
- System errors, component faults and abnormal system operation should be **detected promptly** and the **source** and severity of each malfunction should be **diagnosed** (corrective actions)
- The simultaneous presence of a **physical** substratum and of a **cyber** substratum imposes additional challenges in safety-critical applications

Basic definitions and concepts

Fault Undesired change in the system that tends to degrade overall performance (a fault not necessarily represents a failure of a physical component)

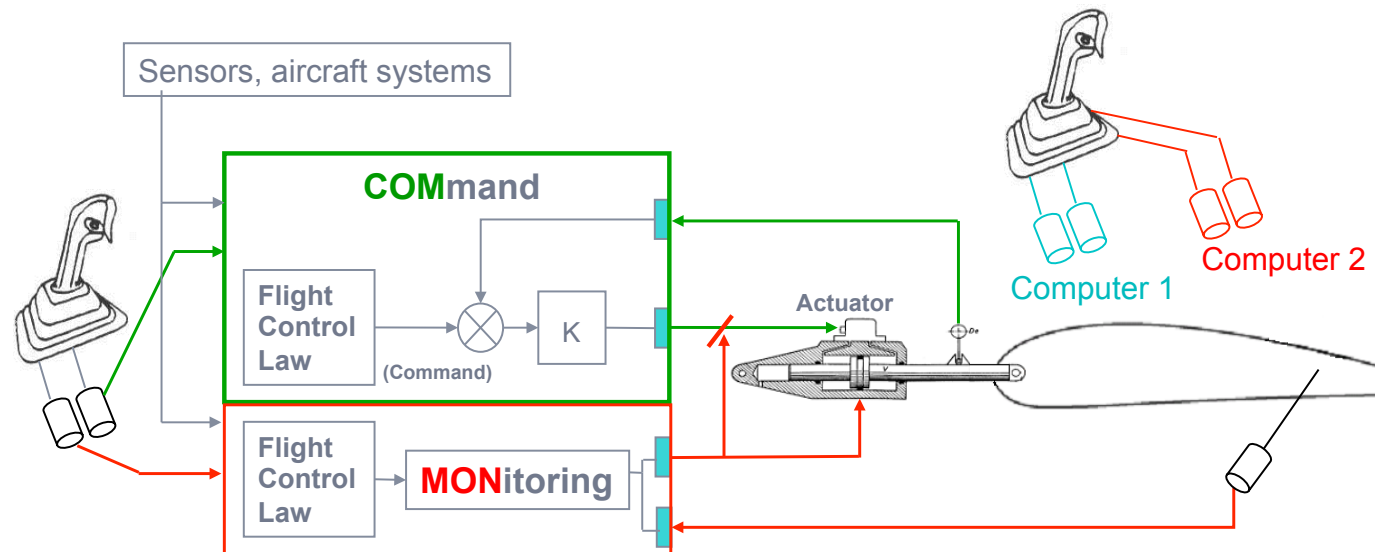
Fault detection Binary decision: “either something has gone wrong or everything is fine”

Fault isolation Determination of the source/type of the fault

Fault diagnosis system Procedure used to detect and isolate faults and possibly assess their significance/severity

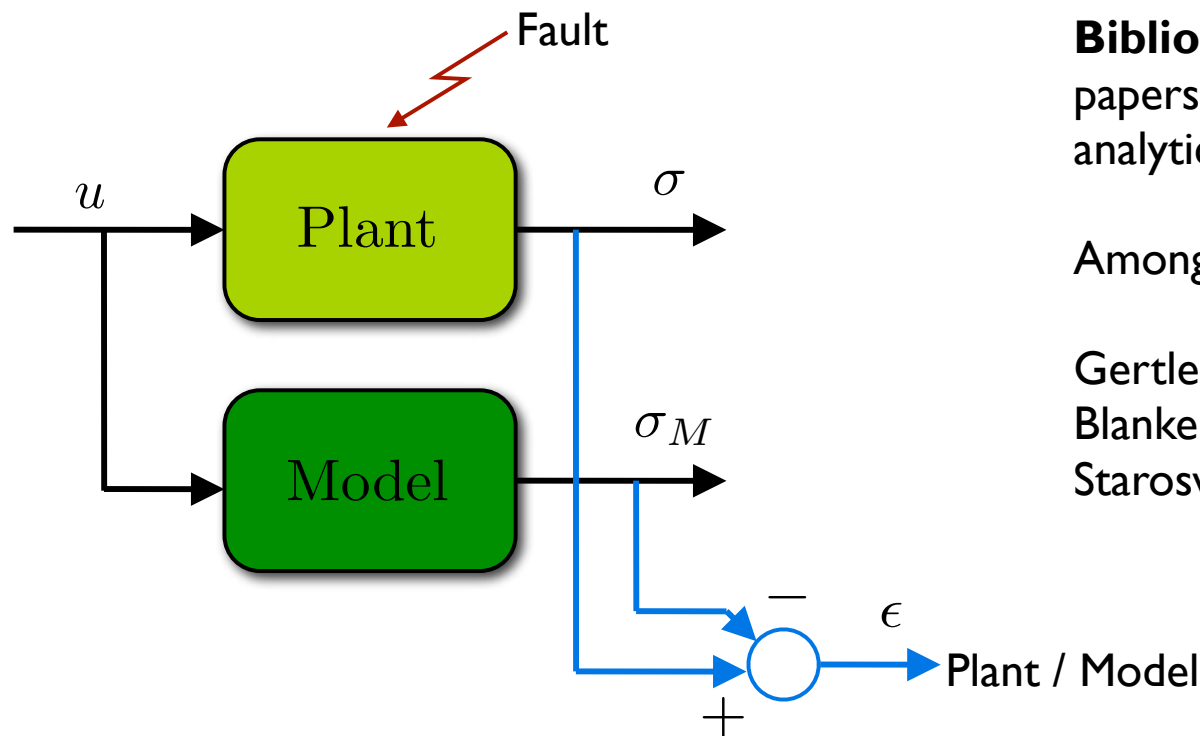
Safety & Fault-tolerance: a step beyond HW redundancy only

Flight Control Computer COM/MOM Airbus Architecture



- Self-checking computers
- Computer switching in case of fault detection

Model-based analytical redundancy: the very basic idea



Bibliography - several books and papers available on FD based on analytical redundancy concept.

Among others:

Gertler 1988; Patton and Chen, 2001;
Blanke, Kinnaert, Lunze and
Staroswiecki, 2003; Isermann, 2006

Key design issues:

- Effects of modelling uncertainties
- Non-conservative diagnosis thresholds

Large-scale CPSs: why distributed?

Mainly because of constraints on:

- **Computation power** needed to handle the global dynamic model (model-based approach)
- **Communications resources** needed to convey the information on all the state variables to a single location

Moreover:

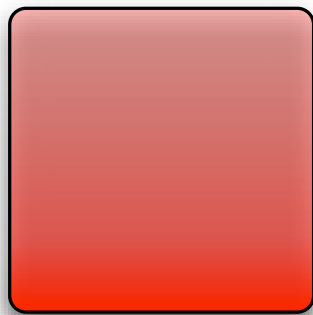
- FDI task running on a single computation node is not fault tolerant itself, nor a single node for this task can always be identified
- The physical substratum may be **spatially distributed**: the notion of locality induced by the physical substratum is not necessarily compatible with the notion of locality induced by the network of sensors (*Tabuada, 2006*)



Layer of networked local monitoring modules

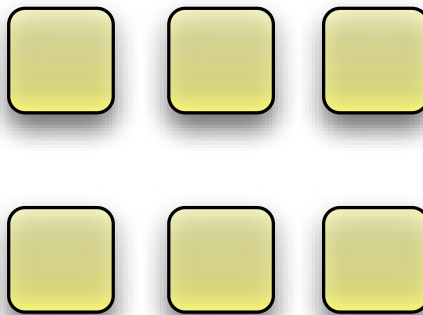
De/centralised, distributed system

System: entity to be monitored against faults



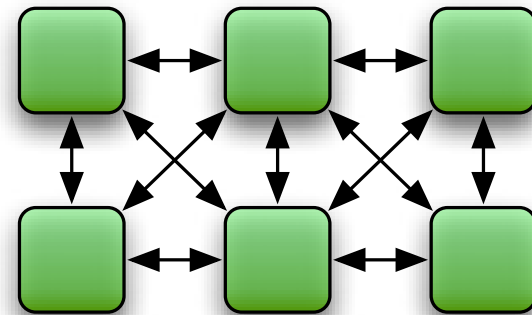
Centralised

Possibly large # of
sub-systems with
global interaction



Decentralised

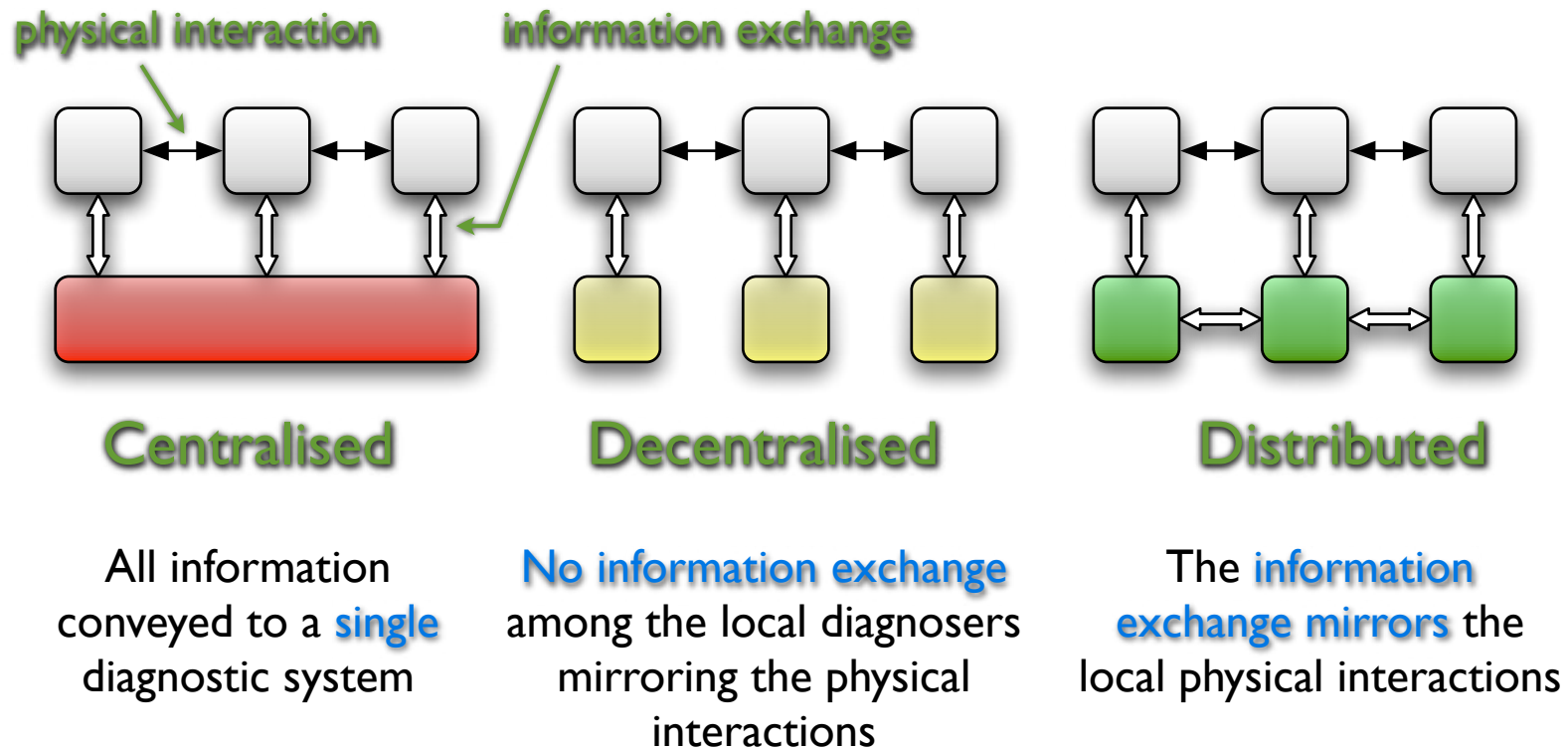
Non-interacting
sub-systems



Distributed

Sub-systems with
local interaction

De/centralised, distributed FD architecture



Distributed FDI: *divide et impera*

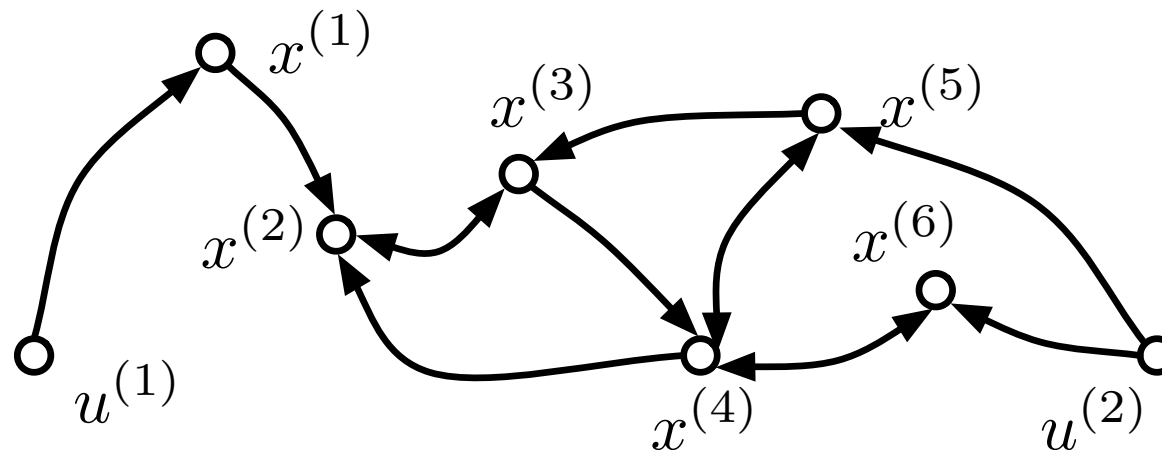
- Convenient to **decompose** the FDI task in smaller sub-tasks that can run in parallel on different local diagnosers
- Use of **directed graphs** to match the decomposition structure
- FDI task decomposition follows from a **decomposition** of the monolithic system **structural graph** and **model**
- **Consensus** techniques used to monitor **overlapping** parts
- **Adaptive approximators** used to **learn** on-line **uncertain** parts of the **model** (typically, the interconnection between subsystems)

A simple structural graph

$$\mathcal{G} \triangleq \{\mathcal{N}_{\mathcal{G}}, \mathcal{E}_{\mathcal{G}}\}$$

- Nodes represent state or input components of the monolithic system
- Two nodes are connected if the first one appears in the state equation of the second one

$$\mathcal{E}_{\mathcal{G}} \triangleq \left\{ (x^{(i)}, x^{(j)}) : "x^{(i)} \text{ acts on } x^{(j)}" \right\} \cup \left\{ (u^{(i)}, x^{(j)}) : "u^{(i)} \text{ acts on } x^{(j)}" \right\}$$



A simple graph decomposition

Local state variables

$$x_1 = [x^{(1)}, x^{(2)}, x^{(3)}]^\top$$

$$x_2 = [x^{(3)}, x^{(4)}, x^{(5)}, x^{(6)}]^\top$$

Local input variables

$$u_1 = u^{(1)}$$

$$u_2 = u^{(2)}$$

Interconnection variables

$$z_1 = [x^{(4)}, x^{(5)}]^\top$$

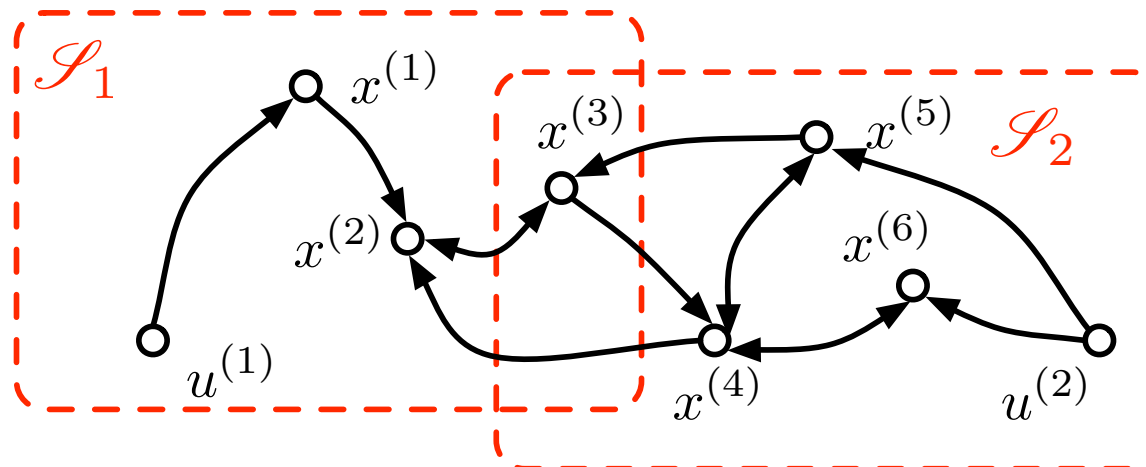
$$z_2 = x^{(2)}$$

Shared variables

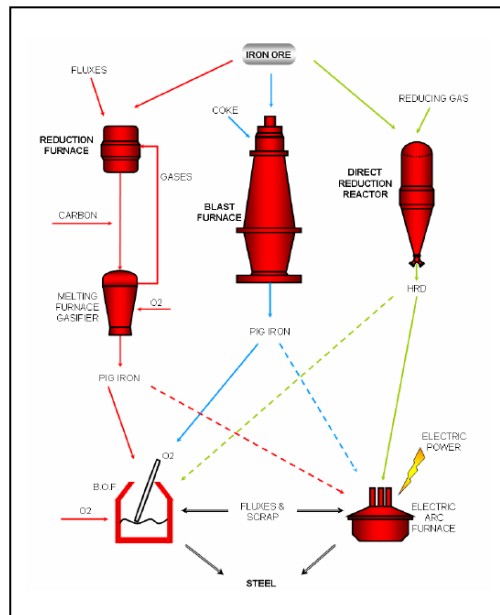
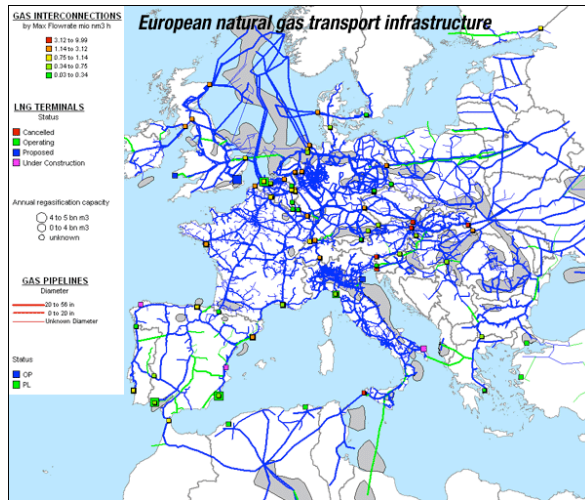
$$x^{(3)} \equiv x_1^{(3)} \equiv x_2^{(1)}$$

Overlap set

$$\mathcal{O}_3 = \{1, 2\}$$



Large-scale CPS “monolithic” model of physical substratum



Nominal model dynamics
(healthy mode)

Modelling uncertainty
(plant/model mismatch)

$$x^+ = \phi(x, u) + \eta(x, u, t) + \mathcal{B}(t - T_0)f(x, u)$$

Time-evolution
of the fault

Deviation to state equation
due to a fault/malfunction.
Several failure causes (e.g.,
component-level, sensors,
but ... malicious too)

Decomposition

We decompose

$$x^+ = \phi(x, u) + \eta(x, u, t) + \mathcal{B}(t - T_0)f(x, u)$$

as

$$x_I^+ = \phi_I(x_I, u_I) + g_I(x_I, z_I, u_I) + \beta(t - T_0)f_I(x_I, z_I, u_I)$$



Nominal local
model dynamics



Interconnection
function (includes
modelling uncertainty)



Local fault dynamic
influence
(modelling of faults)

with $I \in \{1, \dots, N\}$ and

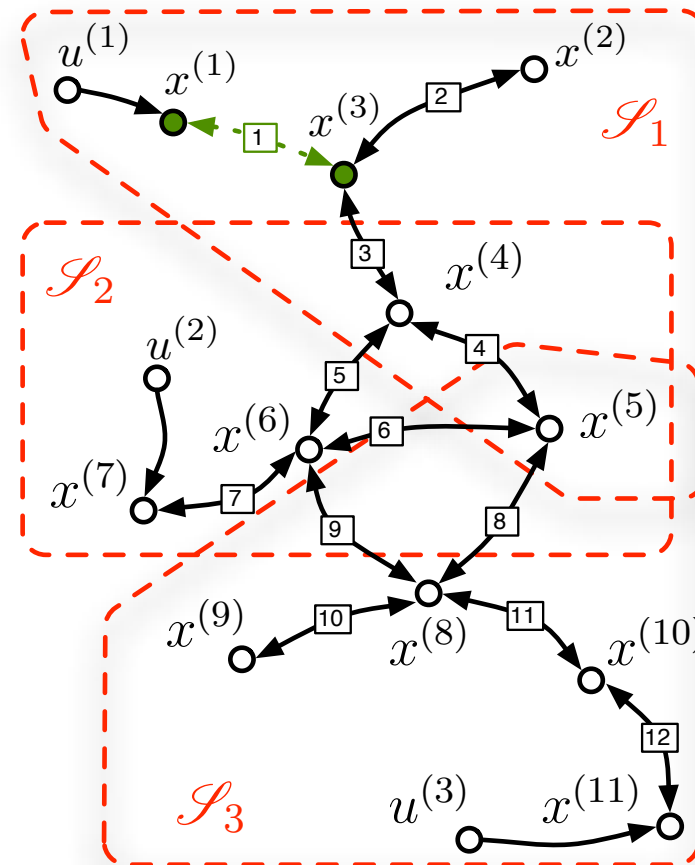
$$f_I(x_I, z_I, u_I) \in \mathcal{F}_I = \{f_I^1(x_I, z_I, u_I), \dots, f_I^{N_{\mathcal{F}_I}}(x_I, z_I, u_I)\}$$

Types of fault: local

- Example of a **local fault**
- **Green arcs** and **nodes** represent the fault influence
- The **influence set** is a singleton

$$\mathcal{U} = \{1\}$$

- Only one LFD (the first one) is needed to detect and isolate the fault



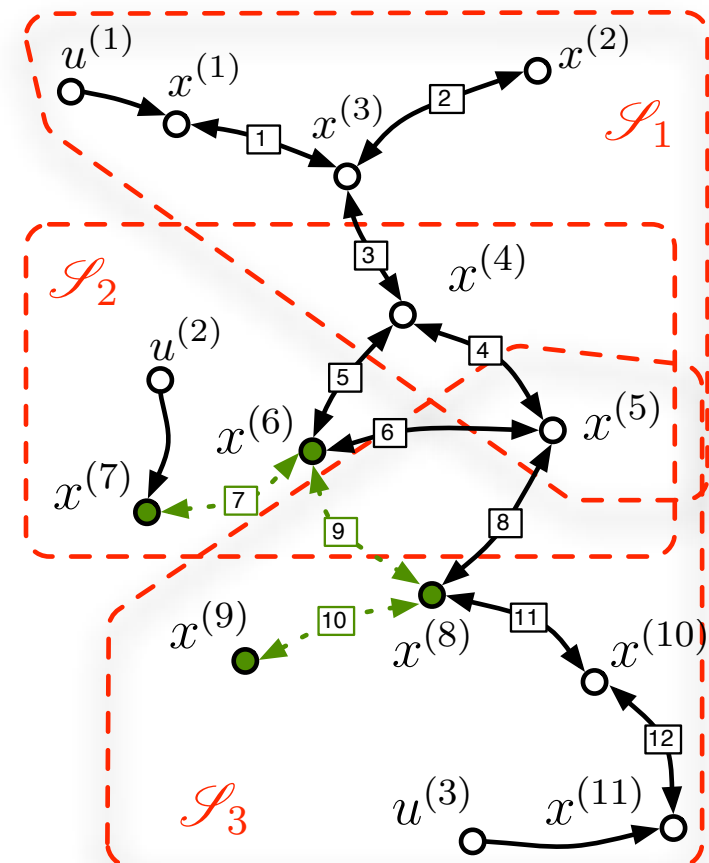
Types of fault: distributed

- This is an example of a **distributed fault**, the fault influence set is

$$\mathcal{U} = \{2, 3\}$$

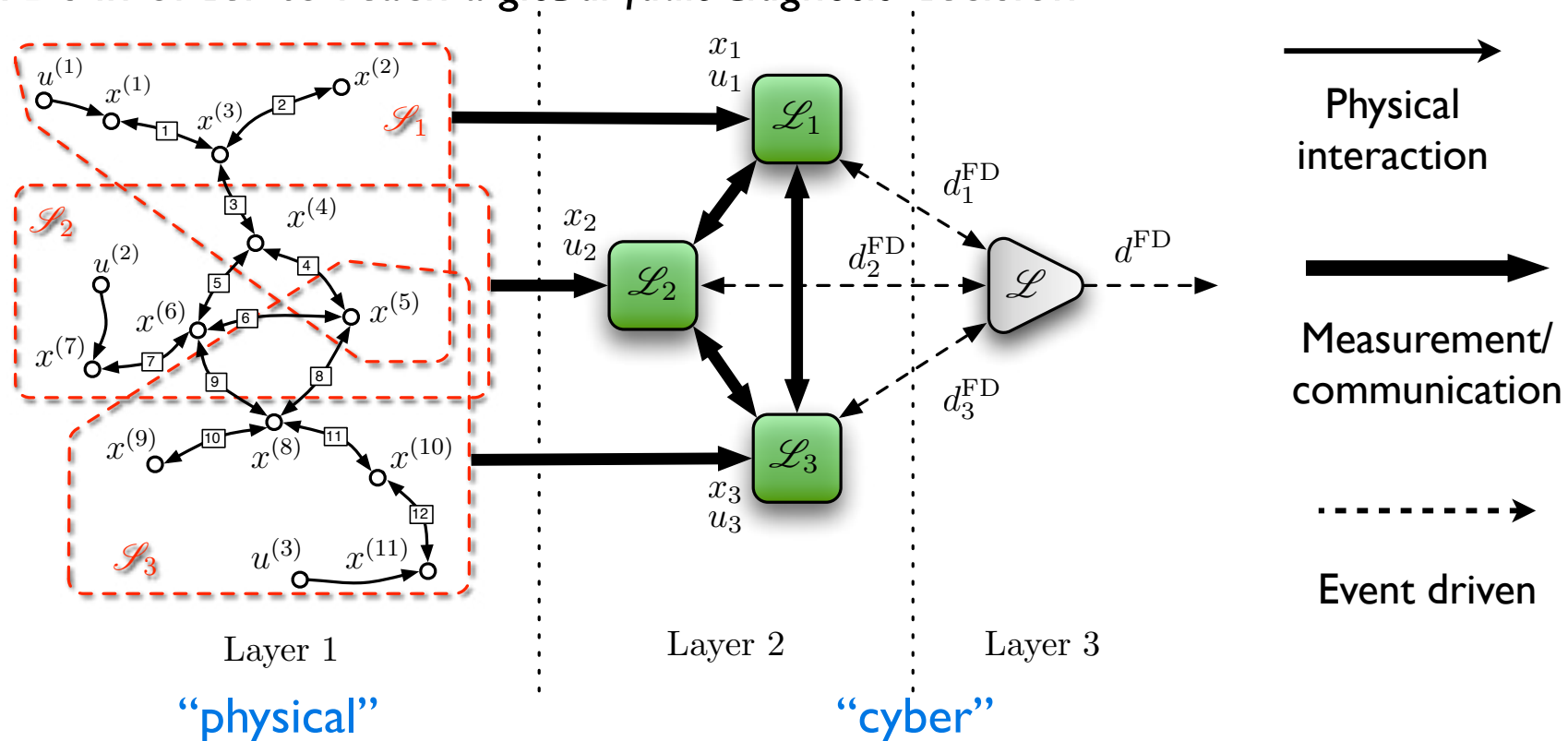
- The fault is **detected** as soon as any LFD locally detects it
- After detection every LFD starts the isolation procedure
- The fault is **isolated** only if all the LFD belonging to \mathcal{U} succeed in isolating their **local component** of the fault

The global isolation is possible thanks to the **GFD**

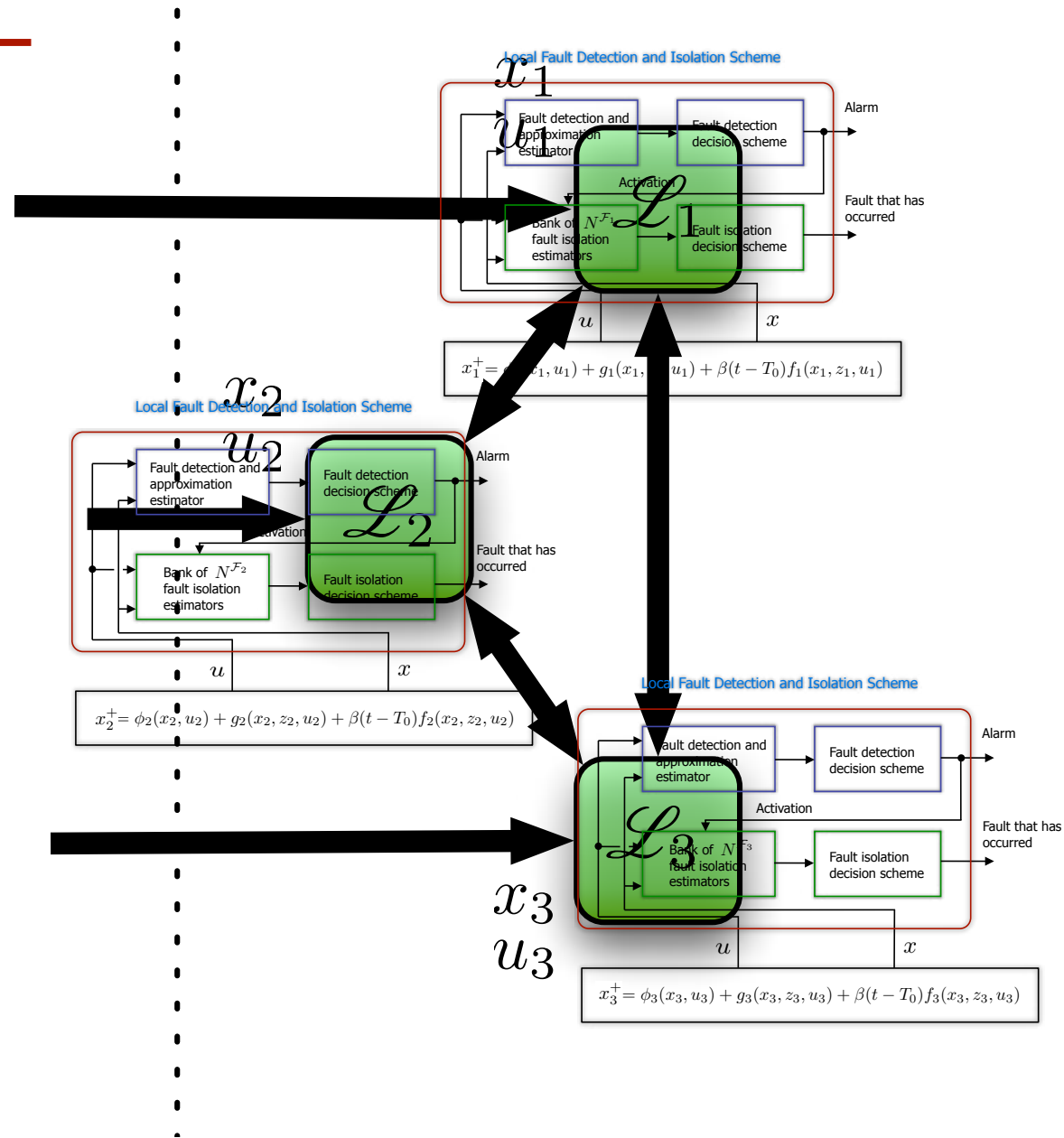


Distributed FDI Architecture

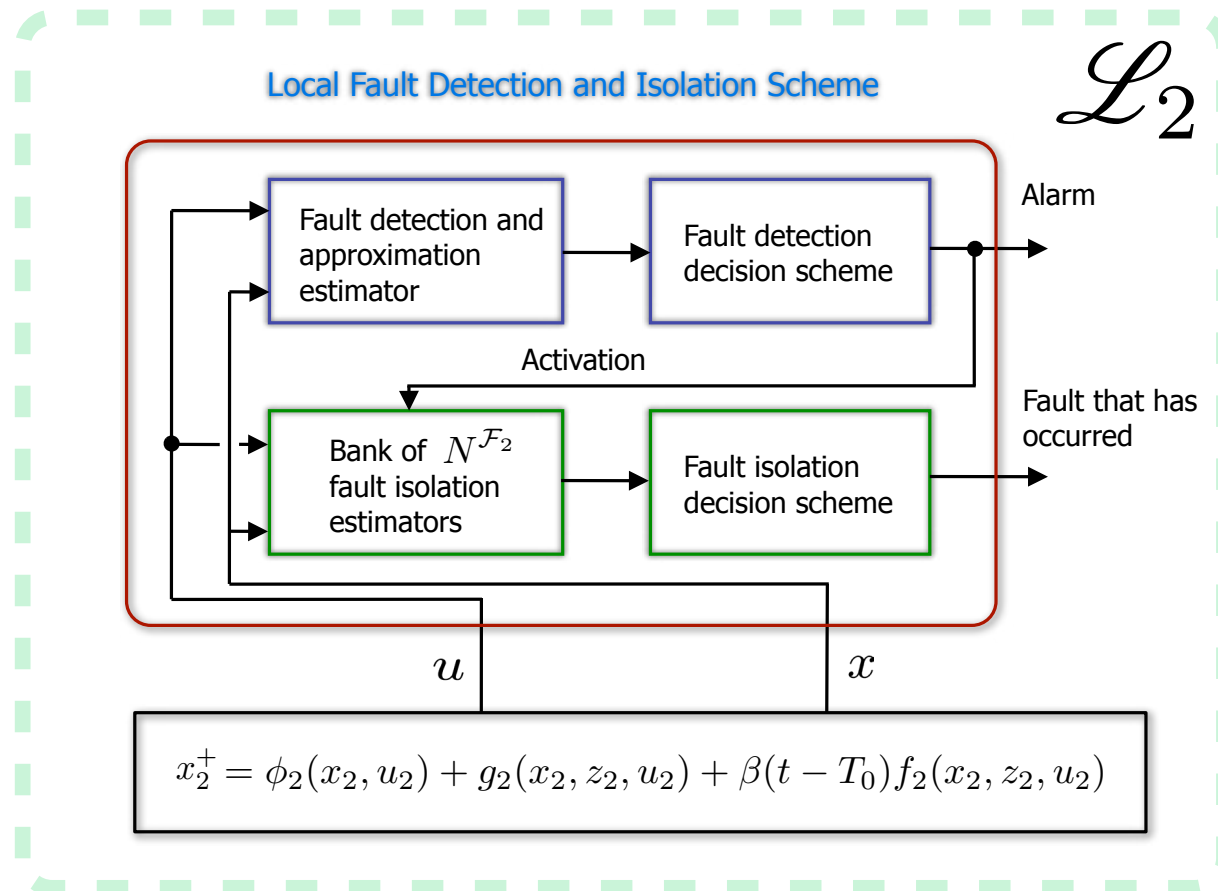
- **Layer 1:** **physical** subsystems
- **Layer 2:** a **Local Fault Diagnoser (LFD)** for each subsystem, using *local measurements* and *exchanging information* with neighbors
- **Layer 3:** a **Global Fault Diagnoser (GFD)** exploiting local fault decisions from LFDs in order to reach a *global fault diagnosis* decision



Distributed FDI Architecture

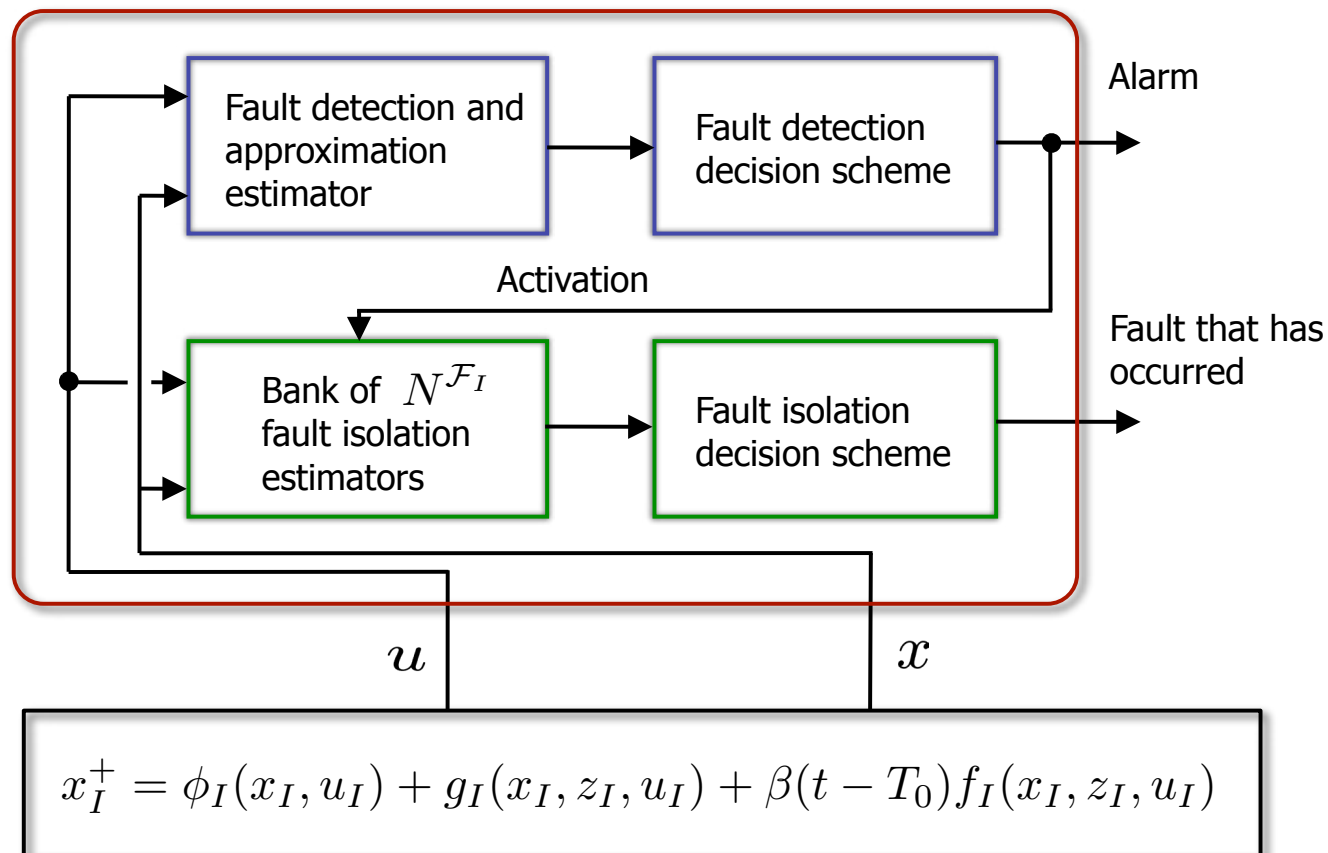


Distributed FDI Architecture



Local FDI architecture

Local Fault Detection and Isolation Scheme



Fault detection and approximation estimator

$$\hat{x}_I^{+(s_I)} = \lambda(\hat{x}_I^{(s_I)} - y_I^{(s_I)}) + \lambda \sum_{J \in \mathcal{O}_s} W_s^{(I,J)} \left[\hat{x}_J^{(s_J)} - \hat{x}_I^{(s_I)} \right]$$

consensus on shared variables

$$+ \sum_{J \in \mathcal{O}_s} W_s^{(I,J)} \left[\phi_J^{(s_J)}(y_J, u_J) + \hat{g}_J^{(s_J)}(y_J, v'_J, u_J, \hat{v}_J) \right]'$$

consensus on shared variables

on-line parametrized adaptive approximation model

delays/packets drop-out in information exchanged between neighbouring diagnosers

Learning algorithm

$$\hat{\vartheta}_I^+ = \mathcal{P}_{\hat{\Theta}_I} \left[\hat{\vartheta}_I + \gamma_I H_I^\top [\epsilon_I^+ - \lambda \epsilon_I] \right]$$

where:

$\mathcal{P}_{\hat{\Theta}_I}$ projection operator on compact set $\hat{\Theta}_I$

$\epsilon_I = y_I - \hat{x}_I^{s_I}$ (from $\hat{x}_I^{+(s_I)} = \dots$)

γ_I learning rate matrix

$$H_I^\top = \partial \hat{g}_I / \partial \hat{\vartheta}_I$$

Fault detection

A **local detection threshold** $\bar{\epsilon}_{\bar{i}}^0(t)$ can be designed depending on a number of important quantities like, for example, bounds on **local modelling uncertainties**, etc.

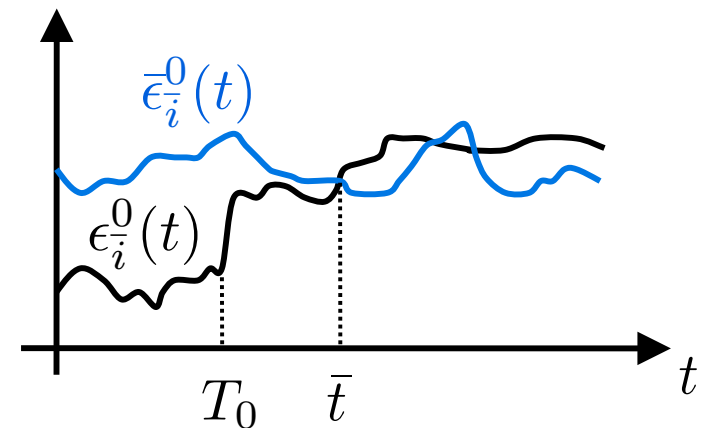
Fault detected if:

$$\exists \bar{i} \in \{1, \dots, n\}$$

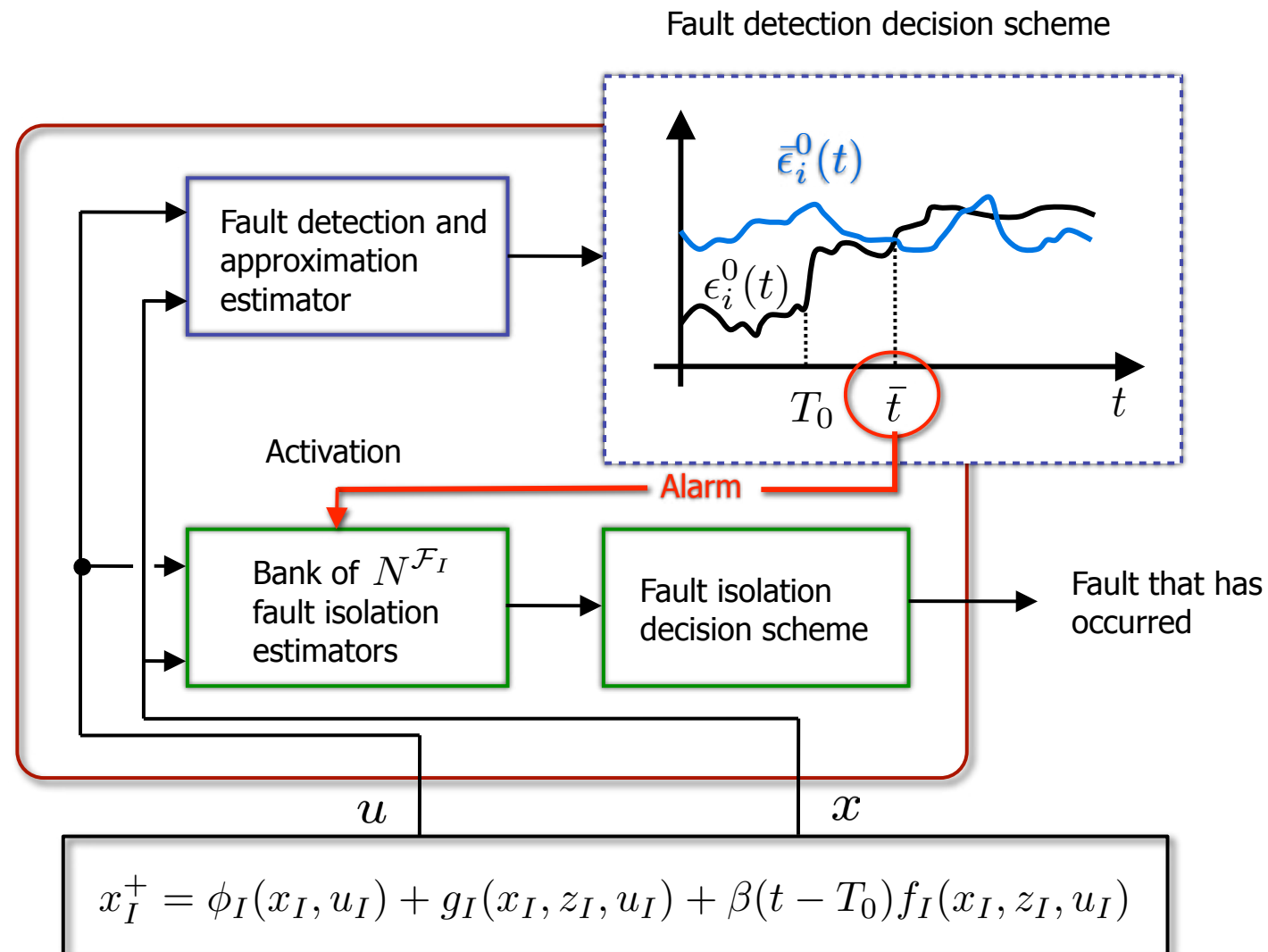
and

$$\exists \bar{t}$$

such that $|\epsilon_{\bar{i}}^0(\bar{t})| > \bar{\epsilon}_{\bar{i}}^0(\bar{t})$



Local detection of a fault activates the isolation phase



Local fault isolation

Fault s isolated if:

$$\forall r \in \{1, \dots, n\} \setminus \{s\}$$

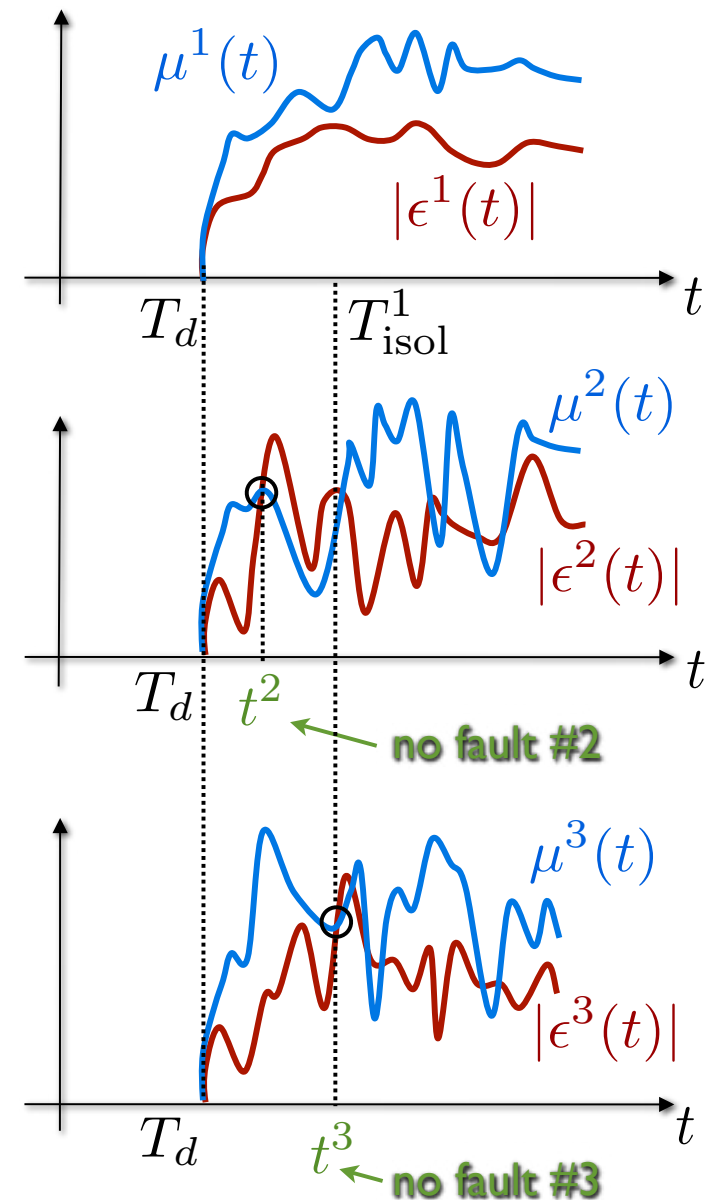
$$\exists \bar{i} \in \{1, \dots, n\}$$

and

$$\exists t^r \geq T_d$$

$$\text{such that } |\epsilon_{\bar{i}}^r(t^r)| > \mu_{\bar{i}}^r(t^r)$$

Three-faults scalar example



Direct Reduction Steel Plant

- Chemical plant for turning iron ore into ~94% pure iron
- Technology born in the '70s
- World production rose from 0.7 to 64 Mt/year (currently 6% of total iron production - steadily increasing)
- More economical and environment friendly than blast furnaces (40-60% less CO₂)

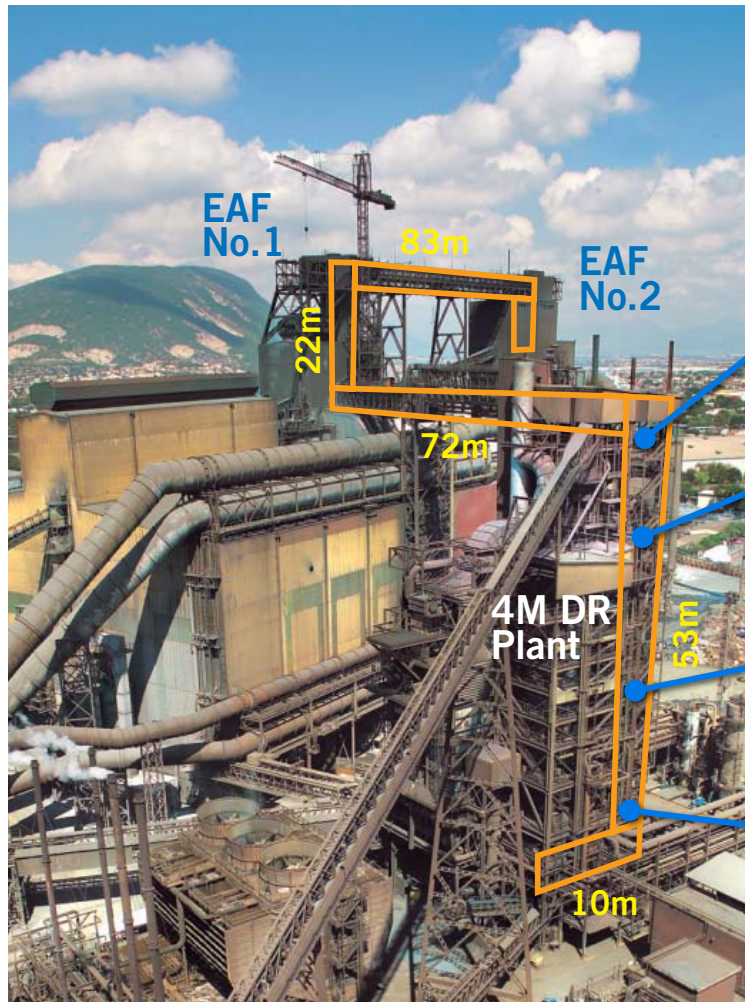


Direct Reduction Steel Plant

- Typical production: 200 t/hour, worth about 100.000 Euro/hour
- Energy consumption: 600 MW, mainly from natural gas
- Time needed for a stop&start: 3 days
- Economical loss caused by a forced maintenance stop due to a fault: about 6 MEuro



Direct Reduction Steel Plant



diameter = 10 m

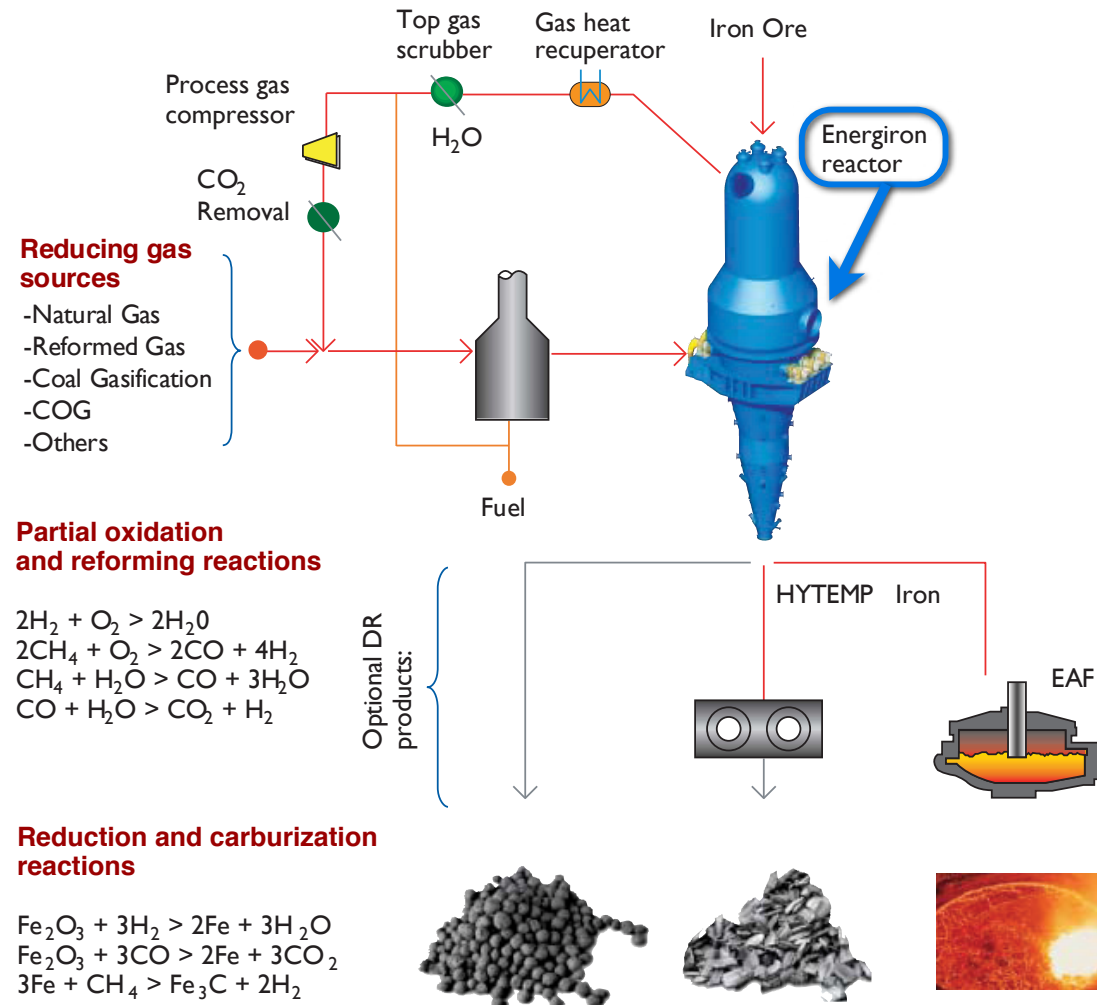


height = 53 m

Courtesy: Tenova-HYL

Simplified layout

- Main component: reduction shaft reactor (height ~ 40 m, diameter ~ 10 m)
- Internal pressure ~ 6 bar, internal temperature ~ 1050 C
- Distributed-parameters, highly nonlinear “multi-physics” system
- pellet flow + gas flow + heat transfer + chemical reactions



Reactor: Modelling for FD

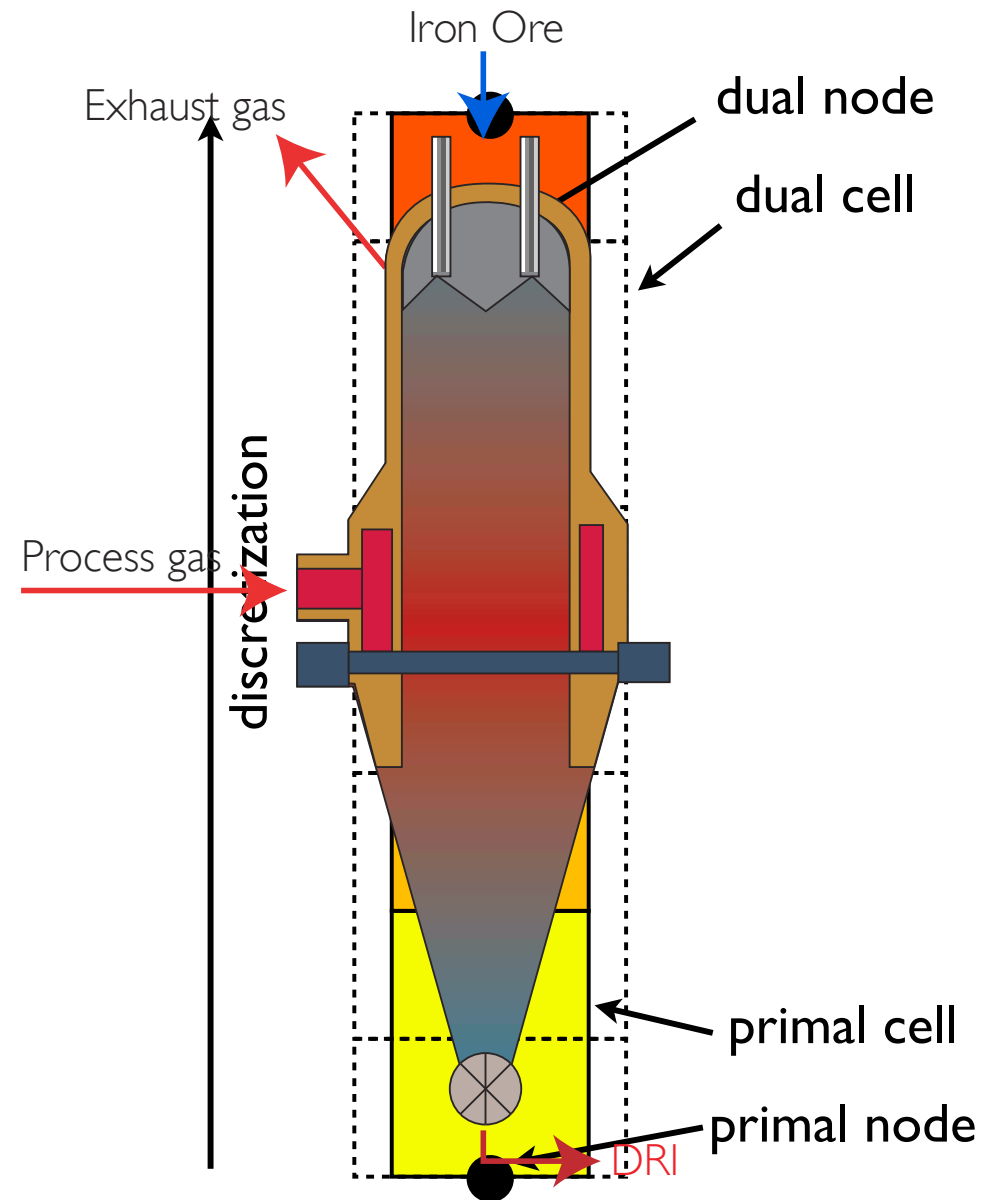
“Unusual” modelling paradigm

Cell method: discrete formulation of Field Laws:

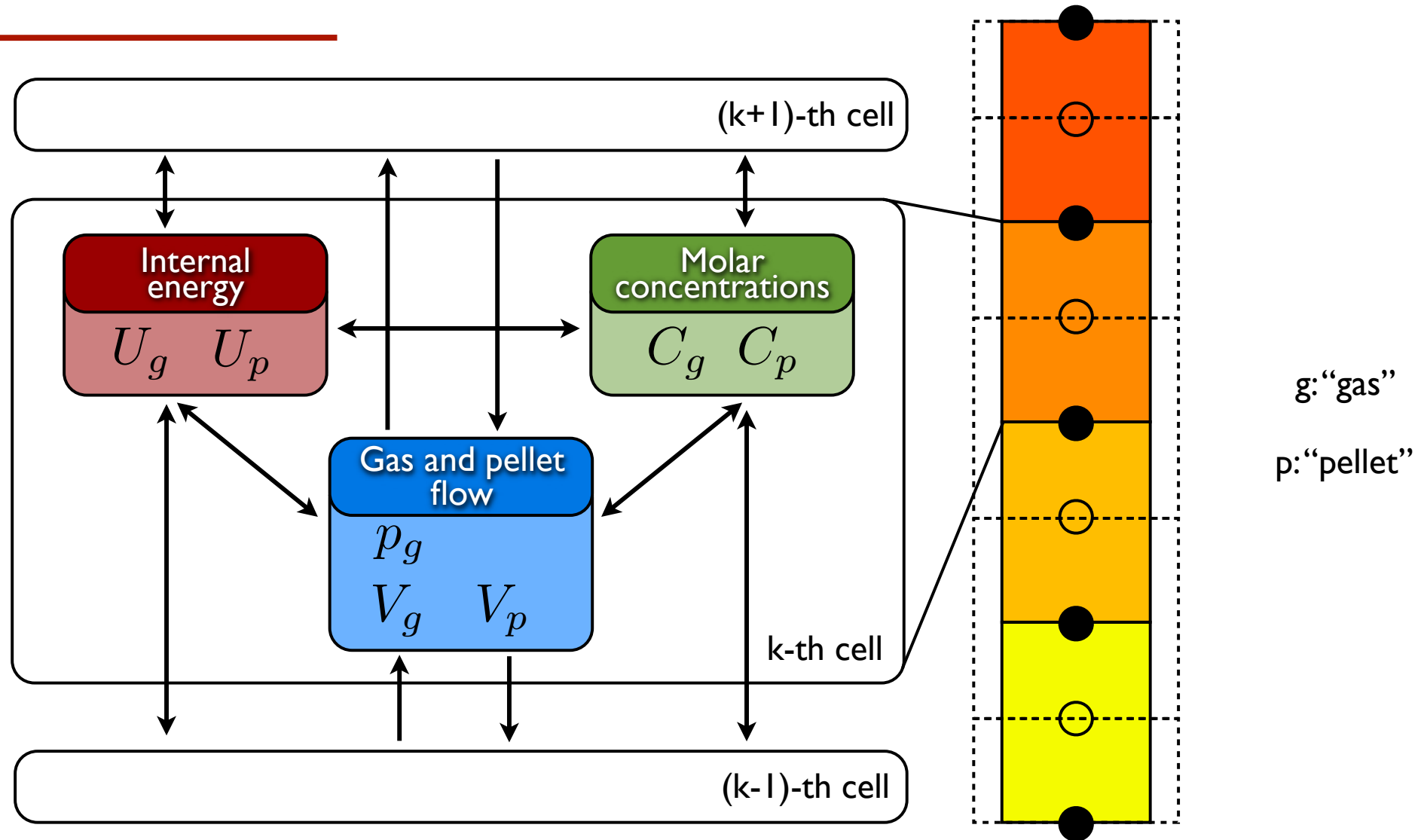
discrete equations defined on two staggered grids:

- first grid: primal cells
- second grid: dual cells

E. Tonti, “A Direct Discrete Formulation of Field Laws: The Cell Method,” *CMES*, vol.2, no.2, pp.237-258, 2001.



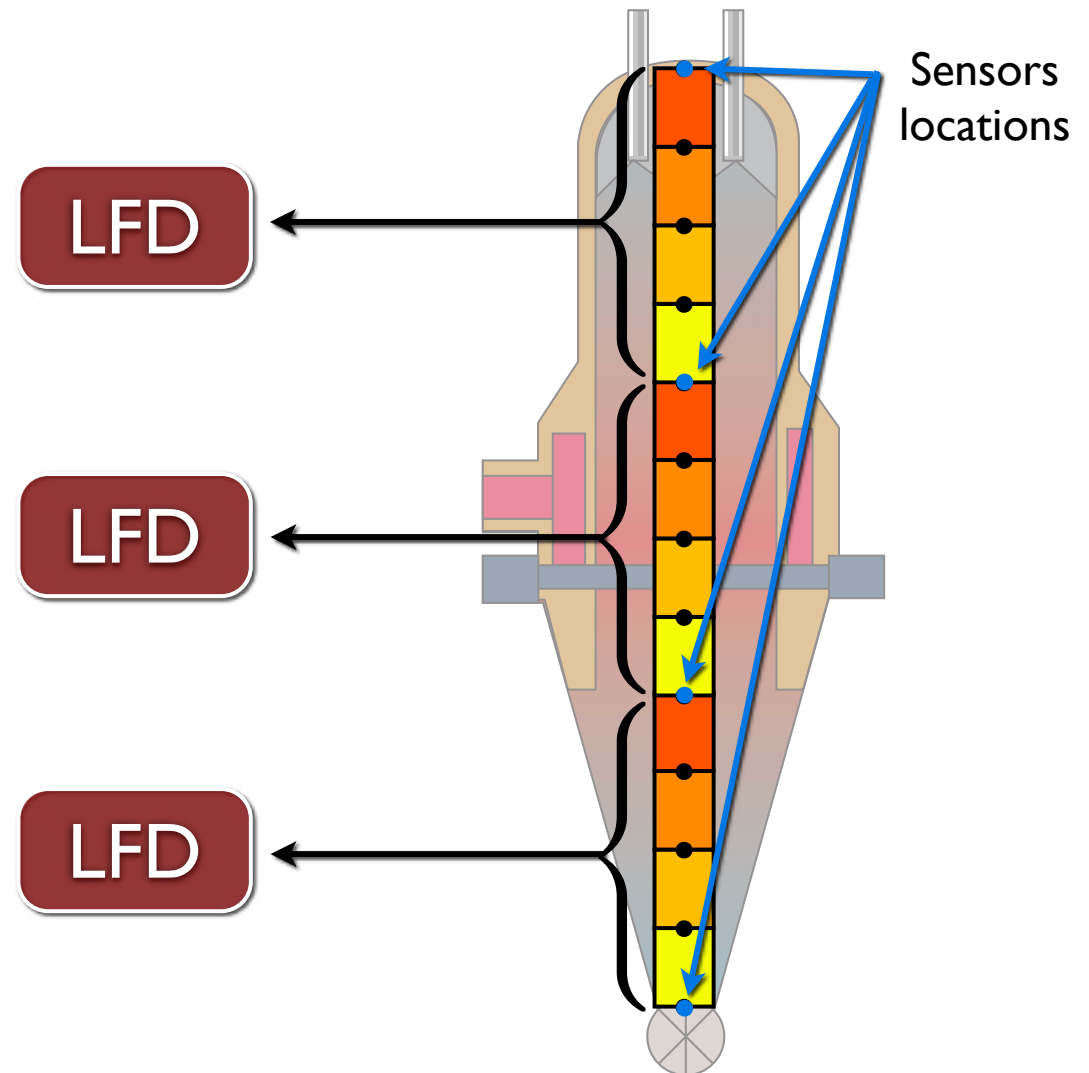
Inside a cell



Distributed FD of the DRI reactor

Key point:

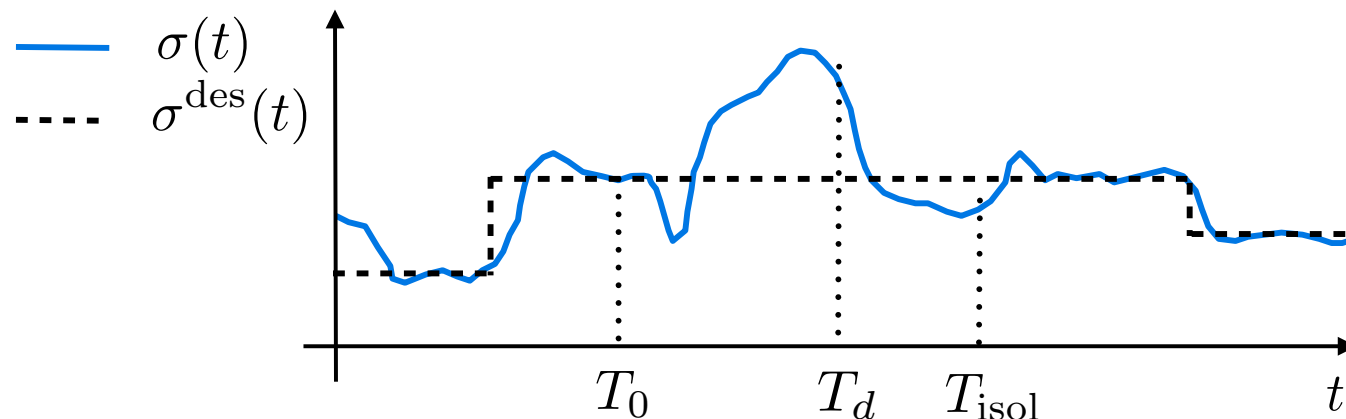
the discrete-cell model “imposes” the decomposition of the large scale system into “strings” of cells between measurement locations



Remarks

What I did not tell you:

- Theoretical results available on **distributed** fault **detectability** and **isolability** [Ferrari et al, *IEEE TAC* 2012, Boem et al., *EJC* 2011]
- **Fault-tolerant control** schemes integrating the FD methodology with reconfigurable controllers are available for local sub-systems



The extension to the distributed fault-tolerant control problem of CPSs is very challenging. Efforts in this direction are under way.

Concluding remarks

- Safety-critical CSPs: need of effective monitoring and diagnosis methodologies and tools
- Several CPSs are very large-scale spatially distributed systems: need of distributed diagnosis tools with scalability characteristics
- Enormous value comes from exploiting the richness of the ever-increasing amount of available data from sensors (wireless or not)
- On-line approximation/learning: a key enabling factor to achieve effective distributed diagnosis and prognosis